

## Physics 12 Formula Sheet for Final Exam

### Constants

$$k = 8.99 \cdot 10^9 \cdot \frac{\text{N} \cdot \text{m}^2}{\text{C}^2} \quad k = \frac{1}{4 \cdot \pi \cdot \epsilon_0}$$

$$e = 1.602 \cdot 10^{-19} \cdot \text{C}$$

$$\text{mass}_e = 9.11 \cdot 10^{-31} \cdot \text{kg}$$

$$\epsilon_0 = 8.85 \cdot 10^{-12} \cdot \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}$$

$$\lambda = \frac{Q}{L}$$

$$\sigma = \frac{Q}{A}$$

$$\rho = \frac{Q}{\text{Vol}}$$

### Electric Force

$$F = k \cdot \frac{Q_1 \cdot Q_2}{r^2}$$

### Electric Field

$$E = \frac{F}{q} = k \cdot \frac{Q}{r^2} = k \cdot \int \frac{1}{r^2} dQ$$

### Electric Flux (Gauss)

$$\Phi_E = E \cdot A = \int E dA = \frac{Q_{\text{encl}}}{\epsilon_0}$$

### Line of Charge

$$E = \frac{1}{2 \cdot \pi \cdot \epsilon_0} \cdot \frac{\lambda}{r}$$

### Line of Charge: Finite

$$E = \frac{\lambda}{2 \cdot \pi \cdot \epsilon_0} \cdot \frac{L}{r \cdot \sqrt{L^2 + 4r^2}}$$

### Spherical Surface

#### Outside

$$E = \frac{1}{4 \cdot \pi \cdot \epsilon_0} \cdot \frac{Q}{r^2}$$

#### Inside

$$E = 0$$

### Solid Sphere

$$E = \frac{1}{4 \cdot \pi \cdot \epsilon_0} \cdot \frac{Q}{r_0^3} \cdot r$$

where  $r_0$  is radius of sphere  
and  $r$  is distance from center

### Infinite Plane

$$E = \frac{\sigma}{2 \cdot \epsilon_0} = \frac{\rho \cdot d}{2 \cdot \epsilon_0}$$

### Two Parallel Plates

$$E_{\text{left}} = E_{\text{right}} = 0$$

$$E_{\text{inside}} = \frac{\sigma}{\epsilon_0}$$

## DC Circuits

### Series

$$V_{\text{eff}} = V_1 + V_2 + \dots$$

$$Q_{\text{eff}} = Q_1 = Q_2 = \dots$$

$$I_{\text{eff}} = I_1 = I_2 = \dots$$

$$\frac{1}{C_{\text{eff}}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

$$R_{\text{eff}} = R_1 + R_2 + \dots$$

### Parallel

$$V_{\text{eff}} = V_1 = V_2 = \dots$$

$$Q_{\text{eff}} = Q_1 + Q_2 + \dots$$

$$I_{\text{eff}} = I_1 + I_2 + \dots$$

$$C_{\text{eff}} = C_1 + C_2 + \dots$$

$$\frac{1}{R_{\text{eff}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

### Current

$$I = \frac{dQ}{dt}$$

### Resistance

$$V = I \cdot R$$

### Junction Rule

$$I_{\text{in}} = I_{\text{out}}$$

### Power

$$P = I \cdot V = I^2 \cdot R = \frac{V^2}{R}$$

### Resistivity ( $\rho$ )

$$R = \rho \cdot \frac{L}{A}$$

### Loop Rule

$$0 = \sum_{\text{loop}} \xi + \sum_{\text{loop}} (I \cdot R)$$

## RC Circuits

### Time Constant

$$\tau = R \cdot C$$

### EMF

$$\xi = \sum_{\text{loop}} (I \cdot R) + \sum_{\text{loop}} \frac{Q}{C}$$

### Voltage (time)

$$V_{\text{cap}} = \xi \cdot \left(1 - e^{-\frac{t}{R \cdot C}}\right)$$

### Voltage

$$V = I \cdot R = \frac{Q}{C}$$

### Current

$$I = \frac{\xi}{R} \cdot e^{-\frac{t}{R \cdot C}}$$

## Magnetism

### Force: Wire

$$\vec{F} = I \cdot (\vec{L} \times \vec{B}) = I \cdot L \cdot B \cdot \sin(\theta)$$

### Force: Particle

$$\vec{F} = q \cdot (\vec{v} \times \vec{B}) = q \cdot v \cdot B \cdot \sin(\theta)$$

### Electron Mas Ratio

$$\frac{e}{m} = \frac{v}{B \cdot r} = \frac{E}{B^2 \cdot r}$$

### Ampere's Law

$$\int \vec{B} \cdot d\vec{L} = \mu_0 \cdot I_{\text{encl}}$$

### Biot-Savart Law

$$\vec{B} = \frac{\mu_0 \cdot I}{4 \cdot \pi} \int \frac{1}{r^2} d\vec{L} \times \vec{r}$$

### Faraday's Law

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

$$\xi = \int \vec{E} \cdot d\vec{L} = -N \cdot \left( \frac{d}{dt} \Phi_B \right)$$

## Inductance

### Self-Inductance

$$L = N \cdot \frac{\Phi_B}{I}$$

$$\xi = -L \cdot \left( \frac{d}{dt} I \right)$$

### Energy: Inductor

$$U = \frac{1}{2} \cdot L \cdot I^2$$

### Mutual Inductance

$$\Phi_B = L \cdot I + M \cdot I$$

### LC Circuit

$$0 = \frac{Q}{C} - L \cdot \left( \frac{d}{dt} I \right)$$

$$\omega^2 = \frac{1}{L \cdot C}$$

### Energy: Capacitor

$$U = \frac{1}{2} \cdot C \cdot V^2$$

### LR Circuit

$$0 = V_0 - L \cdot \left( \frac{d}{dt} I \right) - I \cdot R$$

$$V_R = V_0 \cdot \left( 1 - e^{-R \cdot L^{-1} \cdot t} \right)$$

### Energy Density

$$u = \frac{1}{2} \cdot \frac{B^2}{\mu_0}$$

### Cyclotron: Radius

$$r = \frac{m \cdot v}{q \cdot B}$$

### Cyclotron: Period

$$T = \frac{1}{f} = \frac{2 \cdot \pi \cdot m}{q \cdot B}$$

## Magnetic Sources

### Solenoid

$$n = \frac{N}{L} \quad B = \mu_0 \cdot n \cdot I$$

### Toroid (Circle Solenoid)

$$B_{\text{in}} = \frac{\mu_0 \cdot N \cdot I}{2 \cdot \pi \cdot r}$$

$$B_{\text{out}} = 0$$

## Electromagnetic Induction

### Moving Conductor

$$\xi = B \cdot L \cdot v$$

$$F = I \cdot L \cdot B = \frac{B^2 \cdot L^2}{R} \cdot v$$

$$P = I^2 \cdot R = \frac{B^2 \cdot L^2 \cdot v^2}{R}$$

### Electric and Magnetic Field

$$\vec{F} = q \cdot (\vec{E} + \vec{v} \times \vec{B})$$

### Torque: Magnetic Dipole Moment

$$\vec{\tau} = N \cdot I \cdot (\vec{A} \times \vec{B}) \quad \vec{\mu} = N \cdot I \cdot \vec{A}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

### Permeability of Free Space

$$\mu_0 = 4 \cdot \pi \cdot 10^{-7} \text{ T} \cdot \frac{\text{m}}{\text{A}}$$

### Infinite Wire

$$B = \frac{\mu_0 \cdot I}{2 \cdot \pi \cdot r}$$

### B-Field Inside Wire

$$B = \frac{\mu_0 \cdot I \cdot r}{2 \cdot \pi \cdot R^2}$$

### Parallel Wires

$$B_1 = \frac{\mu_0 \cdot I_1}{2 \cdot \pi \cdot d} \quad F_2 = \frac{\mu_0 \cdot I_1 \cdot I_2}{2 \cdot \pi \cdot d} \cdot L_2$$

### AC Generator

$$\xi = N \cdot B \cdot A \cdot \omega \cdot \sin(\omega \cdot t)$$

### Transformers

$$\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{N_{\text{out}}}{N_{\text{in}}} \quad I_{\text{in}} \cdot V_{\text{in}} = I_{\text{out}} \cdot V_{\text{out}}$$

## Maxwell's Equations

### Ampere

$$\int \vec{B} \cdot d\vec{A} = \mu_0 \cdot I + \mu_0 \cdot \epsilon_0 \cdot \left( \frac{d}{dt} \Phi_E \right)$$

### Faraday

$$\int \vec{E} \cdot d\vec{L} = \frac{d}{dt} \Phi_B$$

### Gauss

$$\int \vec{E} \cdot d\vec{A} = \frac{Q_{\text{encl}}}{\epsilon_0}$$

### Light

$$c = \lambda \cdot f = \frac{1}{\sqrt{\mu_0 \cdot \epsilon_0}}$$

$$\int \vec{B} \cdot d\vec{A} = 0$$